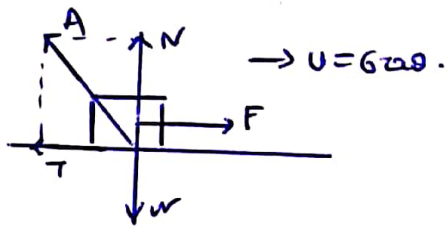


ΘΕΜΑ Α

- A1) β A2) γ A3) δ A4) γ A5) λ, λ, Σ, λ, Σ

ΘΕΜΑ Β



B1)

I)

$$\Sigma F_x = 0 \Rightarrow F = T \Rightarrow T = 6\text{N} \quad \text{και} \quad \Sigma F_y = 0 \Rightarrow N = W \Rightarrow N = 8\text{N}$$

$$A = F_{\text{αντίσω} = \sqrt{N^2 + T^2} = \sqrt{8^2 + 6^2} \Rightarrow A = F_{\text{αντίσω} = 10\text{N} \quad \underline{\Sigma \text{ στο } \tau(\chi)}$$

II)

$$T = \mu \cdot N \Rightarrow 6 = \mu \cdot 8 \Rightarrow \mu = \frac{6}{8} = \frac{3}{4} \Rightarrow \mu = 0,75 \quad \underline{\Sigma \text{ στο } \tau(\chi)}$$

B2)

$$\Sigma F_y = 0 \Rightarrow N = W \Rightarrow N = mg \Rightarrow N = 20\text{N}$$

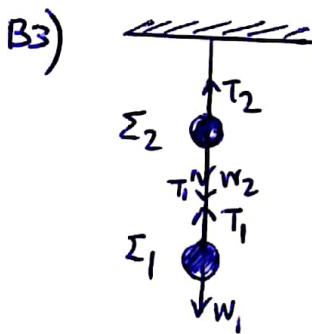
$$T = \mu \cdot N = 0,5 \cdot 20 \Rightarrow T = 10\text{N}$$

$$\Delta x = \frac{1}{2} a \cdot \Delta t^2 \Rightarrow 4 = \frac{1}{2} \cdot a \cdot 2^2 \Rightarrow \boxed{a = 2\text{m/s}^2}$$

$$\Sigma F_x = ma \Rightarrow F - T = ma \Rightarrow F - 10 = 2 \cdot 2 \Rightarrow \boxed{F = 14\text{N}}$$

$$W_F = + F \cdot \Delta x = 14 \cdot 4 \Rightarrow \boxed{W_F = 56\text{J}}$$

$$W_T = - T \cdot \Delta x = -10 \cdot 4 \Rightarrow \boxed{W_T = -40\text{J}}$$

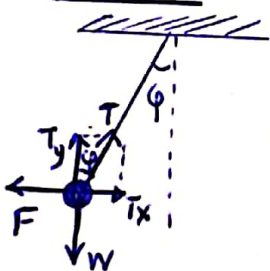


ΣΧΗΜΑ 1

$$\Gamma_{\text{id}} \text{ το } \Sigma_1: \Sigma F = 0 \Rightarrow T_1 = W_1 \Rightarrow \boxed{T_1 = 50\text{N}}$$

$$\Gamma_{\text{id}} \text{ το } \Sigma_2: \Sigma F = 0 \Rightarrow T_2 = T_1' + W_2 \Rightarrow T_2 = 50\text{N} + 100\text{N} \Rightarrow \boxed{T_2 = 150\text{N}}$$

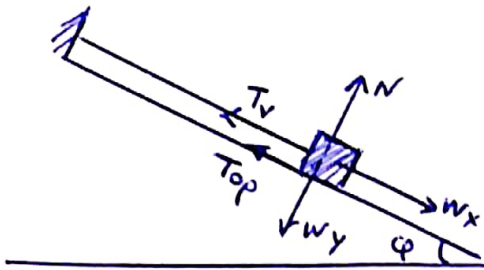
ΣΧΗΜΑ 2



$$\Sigma F_y = 0 \Rightarrow T_y = W \Rightarrow T \sin \varphi = W \Rightarrow T \cdot 0,8 = 100 \Rightarrow \boxed{T = 125\text{N}}$$

$$\Sigma F_x = 0 \Rightarrow T_x = F \Rightarrow T \cos \varphi = F \Rightarrow 125 \cdot 0,6 = F \Rightarrow \boxed{F = 75\text{N}}$$

ΣΧΗΜΑ 3

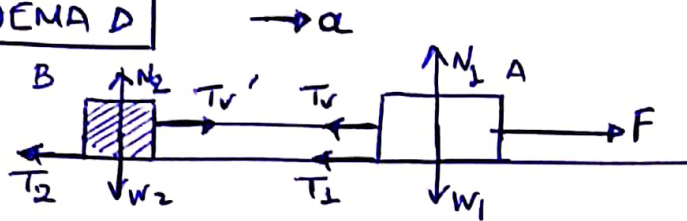


• $\Sigma F_y = 0 \Rightarrow N = W_y \Rightarrow N = W \cdot \sin \varphi \Rightarrow$
 $N = 200 \cdot 0,8 \Rightarrow \boxed{N = 160 \text{ N}}$

• $T_{op} = \mu_s \cdot N = 160 \cdot 0,5 \Rightarrow \boxed{T_{op} = 80 \text{ N}}$

• $\Sigma F_x = 0 \Rightarrow W_x = T_v + T_{op} \Rightarrow$
 $m g \cos \varphi = T_v + T_{op} \Rightarrow 200 \cdot 0,6 = T_v + 80 \Rightarrow$
 $\Rightarrow \boxed{T_v = 40 \text{ N}}$

ΘΕΜΑ D



ΣΟΜΑ A $\Sigma F_y = 0 \Rightarrow N_1 = W_1 \Rightarrow N_1 = m_1 g \Rightarrow N_1 = 30 \text{ N}$

$T_1 = \mu N_1 = 0,5 \cdot 30 \Rightarrow \boxed{T_1 = 15 \text{ N}}$

$\Sigma F_x = m_1 a \Rightarrow F - T_v - T_1 = m_1 a \quad (1)$

ΣΟΜΑ B $\Sigma F_y = 0 \Rightarrow N_2 = W_2 \Rightarrow N_2 = m_2 g \Rightarrow N_2 = 10 \text{ N}$

$T_2 = \mu N_2 = 0,5 \cdot 10 \Rightarrow \boxed{T_2 = 5 \text{ N}}$

$\Sigma F_x = m_2 a \Rightarrow T_v' - T_2 = m_2 a \quad \xrightarrow{T_v' = T_v} T_v - T_2 = m_2 a \quad (2)$

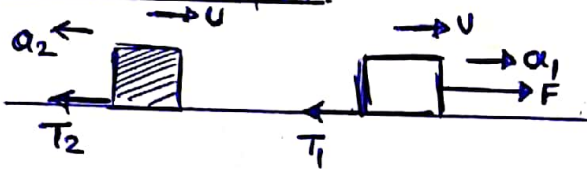
$(1) + (2) \Rightarrow F - T_v - T_1 + T_v - T_2 = m_1 a + m_2 a \Rightarrow F - T_1 - T_2 = (m_1 + m_2) a \Rightarrow$
 $30 - 15 - 5 = (3 + 1) \cdot a \Rightarrow 10 = 4a \Rightarrow \boxed{a = 2,5 \text{ m/s}^2}$

$T_1 + t_1 = 4 \text{ s}$: $U = a \cdot t_1 = 2,5 \cdot 4 \Rightarrow \boxed{U = 10 \text{ m/s}}$

$S = \frac{1}{2} a t_1^2 = \frac{1}{2} \cdot 2,5 \cdot 4^2 \Rightarrow S = 20 \text{ m}$

• Αν τω (2) $\Rightarrow T_v - 5 = 1 \cdot 2,5 \Rightarrow \boxed{T_v = 7,5 \text{ N}}$

Οταν κινεί το σώμα:



ΣΟΜΑ A $\Sigma F_x = m_1 a_1 \Rightarrow F - T_1 = m_1 a_1 \Rightarrow 30 - 15 = 3 a_1 \Rightarrow a_1 = 5 \text{ m/s}^2$

Επειδή $\Sigma F_x \uparrow U$ θα ευρεθεί εύκολα η απόσταση που θα διανύσει το σώμα με $U_{\text{αρχ}} = U = 10 \text{ m/s}$

$T_1 + \Delta t = t_2 - t_1 = 3 \text{ s}$: $S_1 = U_{\text{αρχ}} \cdot \Delta t + \frac{1}{2} a_1 \Delta t^2 = 10 \cdot 3 + \frac{1}{2} \cdot 5 \cdot 3^2 \Rightarrow$
 $S_1 = 30 + 22,5 \Rightarrow S_1 = 52,5 \text{ m}$

ΣΟΜΑ Β

$$\Sigma F_x = m_2 a_2 \Rightarrow T_2 = m_2 a_2 \Rightarrow S = 1 \cdot a_2 \Rightarrow a_2 = 5 \text{ m/s}^2 \quad (\text{Μέτρο επιβραδύνσης})$$

Επειδή $\Sigma \vec{F} \uparrow \downarrow \vec{v}$ θα εκτελέσει ελεύθερη πτώση μέχρι να σταθμώσει μεχρι να σταθμώσει:

$$t_{\text{stop}} = \frac{v_{\text{max}}}{|a_2|} = \frac{10}{5} \Rightarrow t_{\text{stop}} = 2 \text{ s}$$
$$S_{\text{stop}} = \frac{v_{\text{max}}^2}{2|a_2|} = \frac{10^2}{2 \cdot 5} = \frac{100}{10} \Rightarrow S_{\text{stop}} = 10 \text{ m}$$

Το σώμα Β θα έχει σταθμώσει & κινείται την χρονική στιγμή $t = t_1 + t_{\text{stop}} = 4 \text{ s} + 2 \text{ s} \Rightarrow t = 6 \text{ s}$, από την χρονική στιγμή $t_2 = 7 \text{ s}$ θα είναι ήδη ακινητό.

Συνεπώς μετά την θραύση τα μήκη θα διαιρεθούν: $S_2 = S_{\text{stop}} = 10 \text{ m}$.

ΥΠΟΛΟΓΙΣΜΟΣ ΘΕΡΜΟΤΗΤΩΝ

Για το χρονικό διάστημα $0 - t_1$:

$$Q_1 = |W_{T_1}| = T_1 S = 15 \cdot 20 \text{ J} \Rightarrow Q_1 = 300 \text{ J}$$

$$Q_2 = |W_{T_2}| = T_2 \cdot S = 5 \cdot 20 \text{ J} \Rightarrow Q_2 = 100 \text{ J}$$

Για το χρονικό διάστημα $t_1 = 4 \text{ s}$ έως $t_2 = 7 \text{ s}$

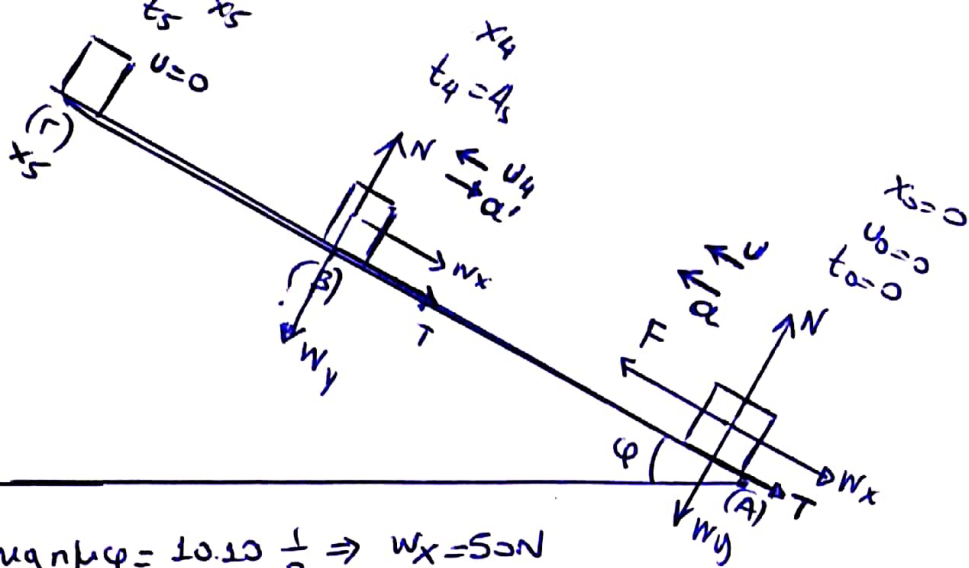
$$Q_1' = |W_{T_1}| = T_1 S_1 = 15 \cdot 52,5 \text{ J} \Rightarrow Q_1' = 787,5 \text{ J}$$

$$Q_2' = |W_{T_2}| = T_2 \cdot S_2 = 5 \cdot 10 \text{ J} \Rightarrow Q_2' = 50 \text{ J}$$

ΣΥΝΟΛΙΚΑ: $Q_{\text{ολ}} = Q_1 + Q_2 + Q_1' + Q_2' = 300 \text{ J} + 100 \text{ J} + 787,5 \text{ J} + 50 \text{ J} \Rightarrow$

$$Q_{\text{ολ}} = 1237,5 \text{ J}$$

ΘΕΜΑ Γ



Γ1.) $W_x = mg \sin \varphi = 10 \cdot 10 \cdot \frac{1}{2} \Rightarrow W_x = 50 \text{ N}$
 $W_y = mg \cos \varphi = 10 \cdot 10 \cdot \frac{\sqrt{3}}{2} \Rightarrow W_y = 50\sqrt{3} \text{ N}$
 $\Sigma F_y = 0 \Rightarrow N = W_y \Rightarrow N = 50\sqrt{3} \text{ N}$
 $T = \mu N = \frac{\sqrt{3}}{3} \cdot 50\sqrt{3} \Rightarrow T = 50 \text{ N}$

Γ2.) $\Sigma F_x = m a \Rightarrow F - W_x - T = m a \Rightarrow 120 - 50 - 50 = 10 a \Rightarrow$
 $\Rightarrow 20 = 10 \cdot a \Rightarrow a = 2 \text{ m/s}^2$

Γ3.) $\Delta x_1 = \frac{1}{2} a \Delta t_1^2 \Rightarrow \Delta x_1 = \frac{1}{2} \cdot 2 \cdot 4^2 \Rightarrow \Delta x_1 = 16 \text{ m} \Rightarrow$
 $x_4 - x_0 = 16 \text{ m} \Rightarrow x_4 - 0 = 16 \text{ m} \Rightarrow x_4 = 16 \text{ m}$

$u_4 = a \cdot \Delta t_1 = 2 \cdot 4 \Rightarrow u_4 = 8 \text{ m/s}$

Γ4.) $W_W^{A \rightarrow B} = W_{W_x}^{A \rightarrow B} = -W_x \cdot \Delta x_1 = -50 \cdot 16 \text{ J} \Rightarrow W_W^{A \rightarrow B} = -800 \text{ J}$
 $W_F = F \cdot \Delta x_1 = 120 \cdot 16 \text{ J} = 1920 \text{ J}$

Γ5.) $\Sigma F_x = m a' \Rightarrow W_x + T = m a' \Rightarrow 50 + 50 = 10 \cdot a' \Rightarrow a' = 10 \text{ m/s}^2$
 $\Delta x_2 = S_{\text{stop}} = \frac{u_{\text{app}}^2}{2|a'|} = \frac{u_4^2}{2|a'|} = \frac{8^2}{2 \cdot 10} = 3,2 \text{ m}$ (Μέτρο επιβραδύνσης)

και

$\Delta x_2 = x_5 - x_4 \Rightarrow x_5 = \Delta x_2 + x_4 \Rightarrow x_5 = 3,2 \text{ m} + 16 \text{ m} \Rightarrow$
 $x_5 = 19,2 \text{ m}$